



WESLEY COLLEGE

By daring & by doing

2018 YEAR 12 MATHEMATICS METHODS

Logarithms & Differentiation Applications

Test 2

Name: _____

Marks: /50

Calculator Free (22 marks)

1. [2, 2 = 4 marks]

The displacement for an object is given by $x = e^{2t} \sin(t)$, where x is in metres and t is in seconds.

a) Determine the velocity equation.

b) Show that when the object is at rest, $\tan(t) = -\frac{1}{2}$

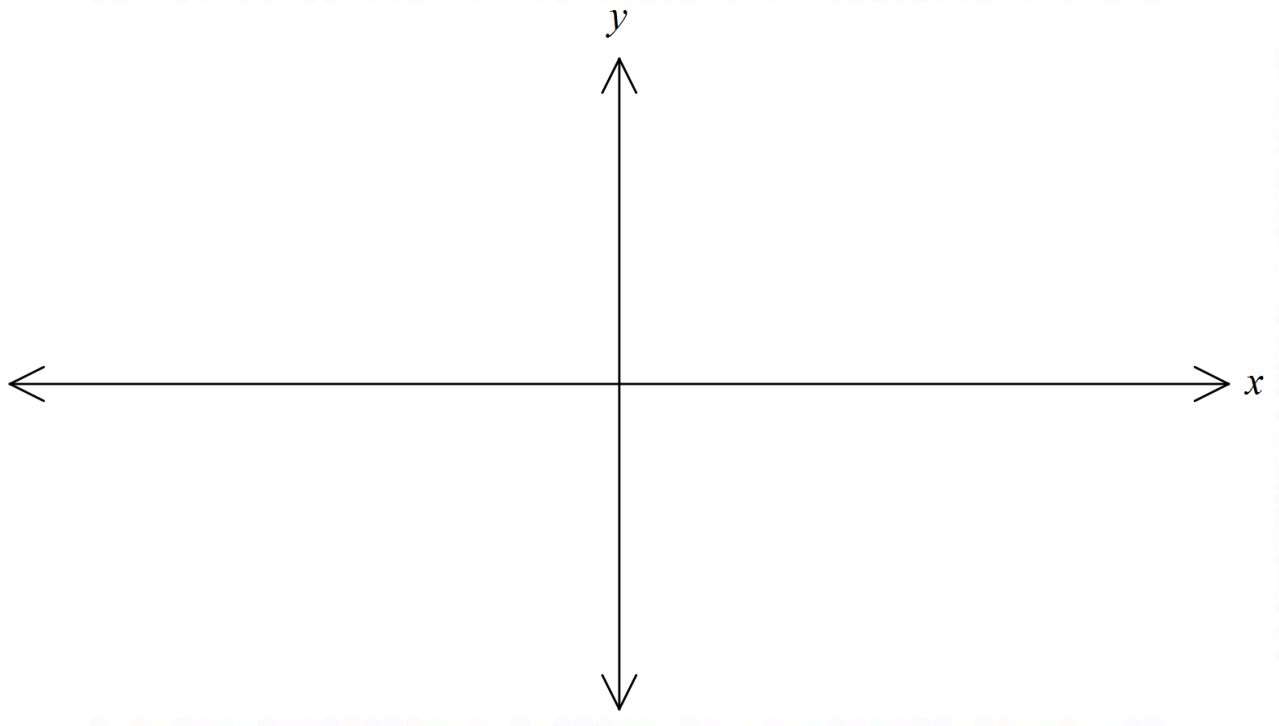
2. [2, 3, 2 = 7 marks]

Given the function: $y = x^4 + 4x^3 - 16x + 3$.

- a) The gradient function, $y' = 4x^3 + 12x^2 - 16$ can be factorised as $y' = 4(x + 2)^2(x - 1)$
By using relevant tests to justify your answers, find and state the nature of all stationary points.

- b) Using relevant tests to justify your answers, find and state all points of inflection.

c) Sketch the graph of $y = f(x)$, showing all important features.



3. [3 marks]

Given that $y = \sqrt{x}$, use the incremental formula $\delta y \approx \frac{dy}{dx} \times \delta x$ to determine an approximate value for $\sqrt{50}$.

4. [2, 2, 4 = 8 marks]

a) Evaluate $\log_x x^2 - 6\log_x y + 3\log_x (xy)^2$

b) Given $2\log_n x - 1 = \log_n 25$, write x in terms of n .

c) If $5^x = 3$ and $5^y = 4$, express in terms of x and/or y :

(i) $\log_5 0.75$

(ii) $\log_5 100$

End of Part A



NAME: _____

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Calculator Section

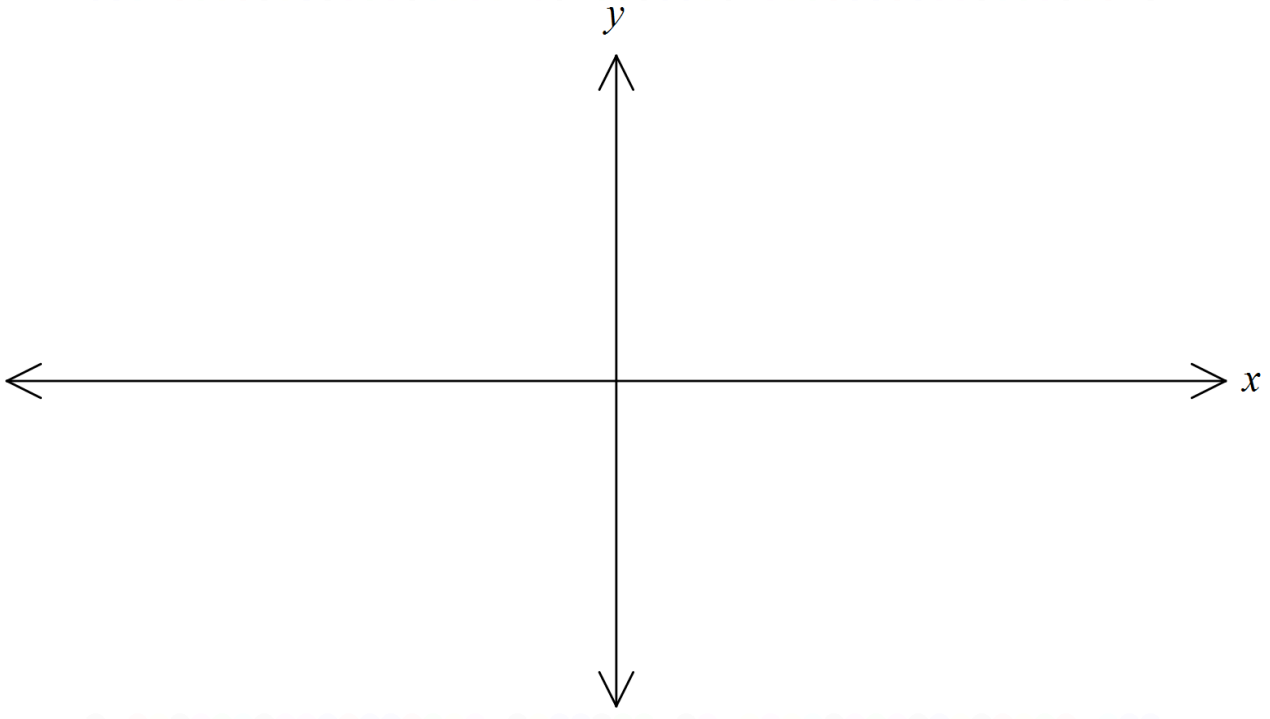
(28 marks)

5. [4 marks]

Draw one possible function with all the following features:

$$\frac{dy}{dx} = 0 \text{ for } x = -3, x = 2, x = 5$$

$$\frac{d^2y}{dx^2} < 0 \text{ for } x = -3 \quad \frac{d^2y}{dx^2} > 0 \text{ for } x = 2 \text{ and } \frac{d^2y}{dx^2} = 0 \text{ for } x = 5$$

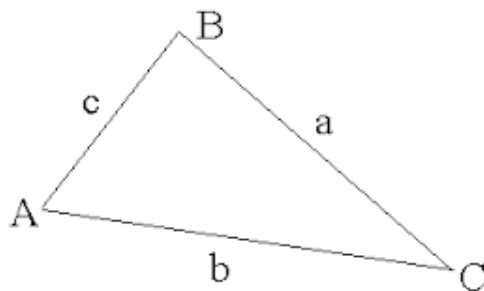


6. [3 marks]

The area of a triangle
formula

can be calculated by the

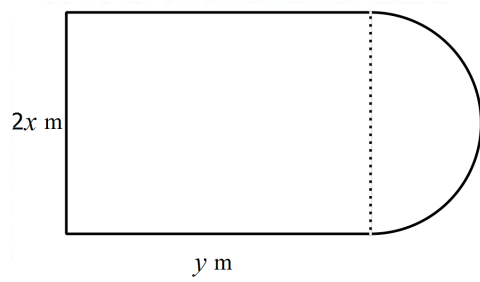
$$Area = \frac{ab \sin C}{2}.$$



Using the incremental formula, determine the approximate change in area of an equilateral triangle, with each side 20 cm, when each side increases by 0.1 cm.

8. [2, 1, 4 = 7 marks]

A 200 m fence is placed around a lawn which has the shape of a rectangle with a semi-circle on one of its sides.



a) Using the dimensions on the diagram, clearly show that $y = 100 - x - \frac{\pi}{2}x$

b) Hence, determine the area of the lawn $A(x)$, in terms of x only.

c) Using calculus techniques determine the dimensions of the lawn if it has a maximum area and state this area.

